



# Integrating Natural and Computer Sciences to Explore the Structure and Dynamics of Complex Ecological Networks

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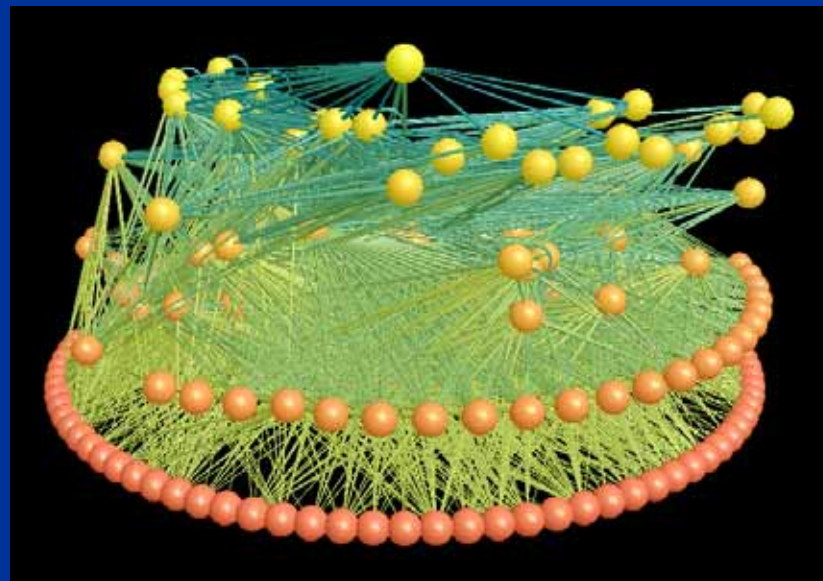
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<sup>3</sup> Ecological Networks Lab, Tech. U. of Darmstadt, Germany



Lake Tahoe food web

Food web graphics  
by Web3D © Rich  
Williams



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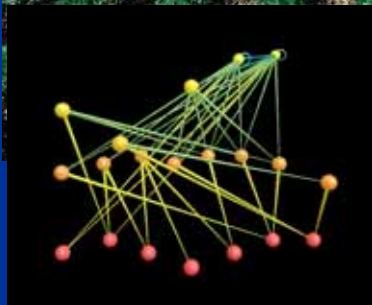
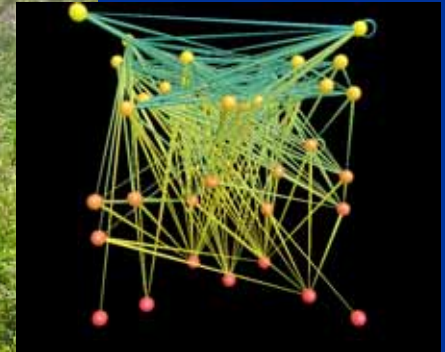
Dalhousie Univ.

**Ilmi Yoon<sup>1</sup>**

San Francisco State U.



**Early paradigm: complex communities are more stable than simple ones (Odum 1953, MacArthur 1955, Elton 1958)**



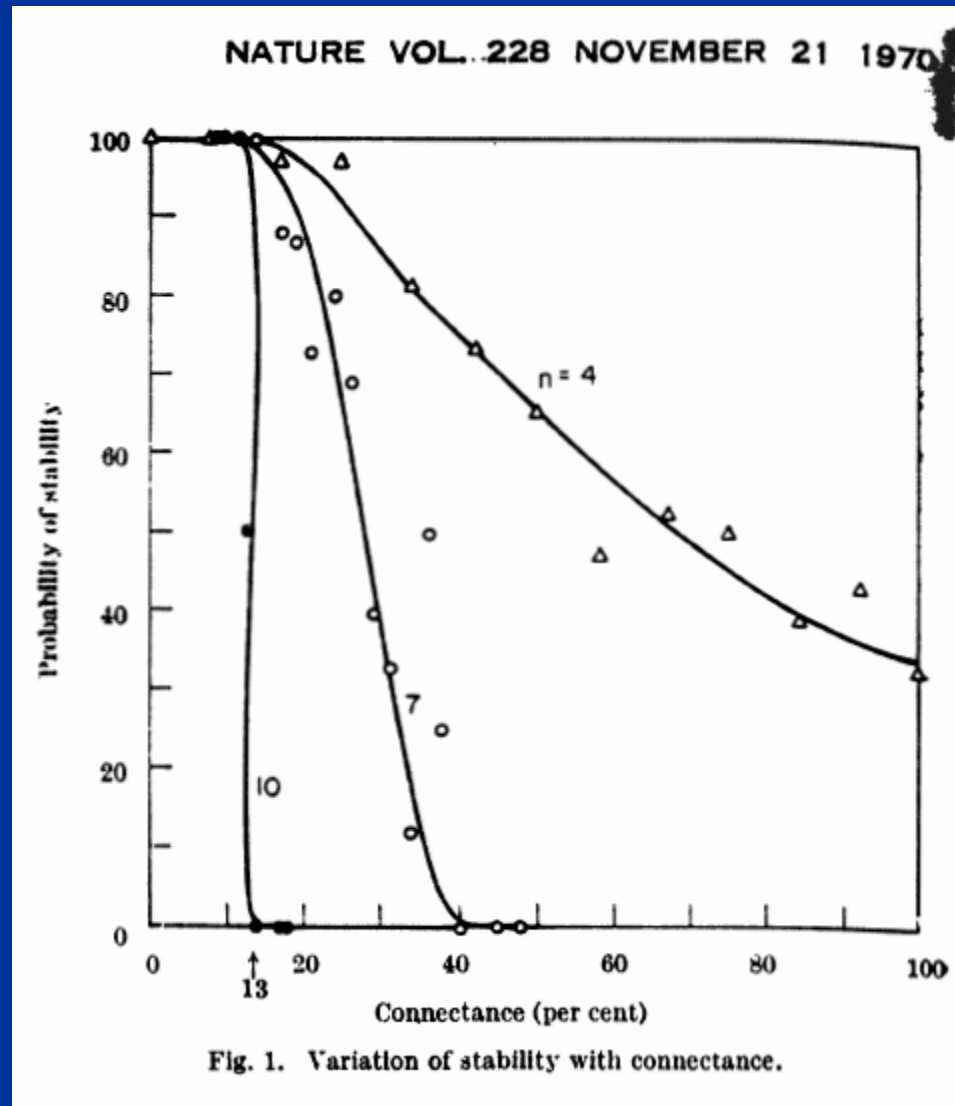
Less invasions,  
less species turnover,  
less calamities,...



## Change of paradigm: Unstable complex systems

Mathematically, stability  
decreases with system  
diversity (species) and  
complexity (interactions)

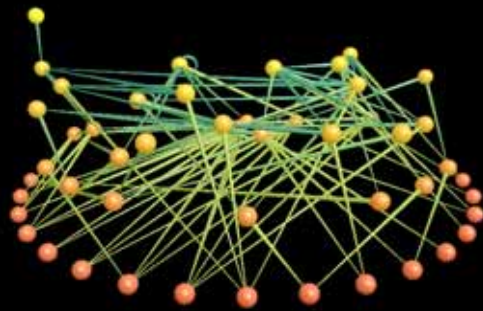
Gardner & Ashby 1970 Nature;  
May 1972 Nature





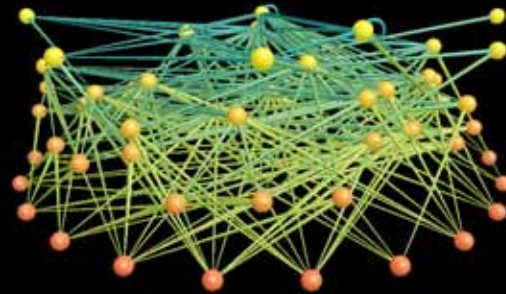
3 “niche model” food webs with  $S = 50$   
and empirically observed range of connectance  
( $C = \text{Links}/\text{Species}^2$ )

$C = 0.03$



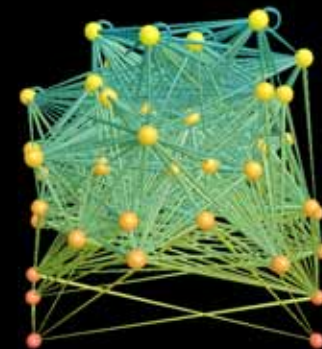
75 links

$C = 0.10$



250 links

$C = 0.30$

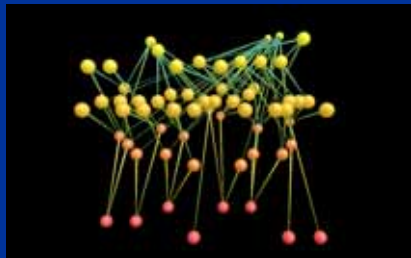


750 links



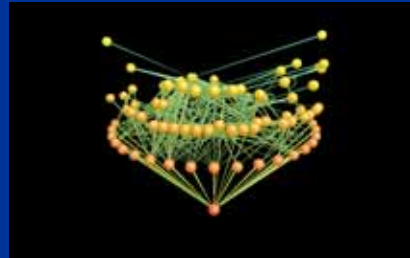
# Low Connectance Webs, $C < 0.10$

UK Grassland



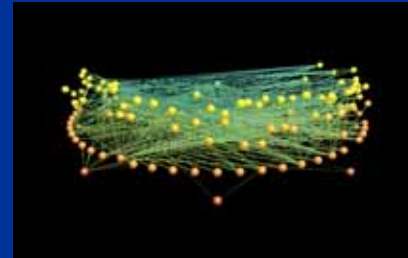
$C = 0.03$ ,  $S = 61$ ,  $L/S = 1.6$   
Martinez et al. 1999

Scotch Broom



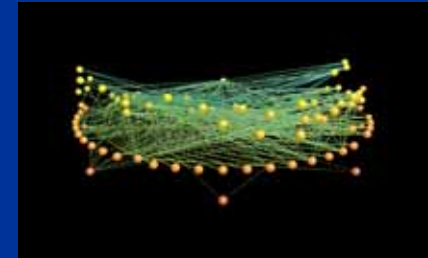
$C = 0.03$ ,  $S = 85$ ,  $L/S = 2.6$   
Memmott et al. 2000

Ythan Estuary



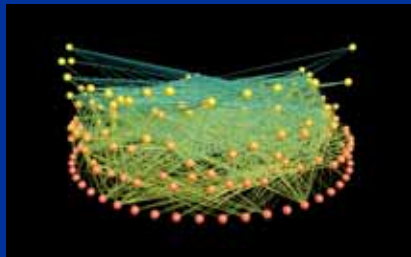
$C = 0.04$ ,  $S = 124$ ,  $L/S = 4.7$   
Huxham et al. 1996

Ythan Estuary, no parasites



$C = 0.06$ ,  $S = 83$ ,  $L/S = 4.8$   
Hall & Raffaelli 1991

El Verde Rainforest



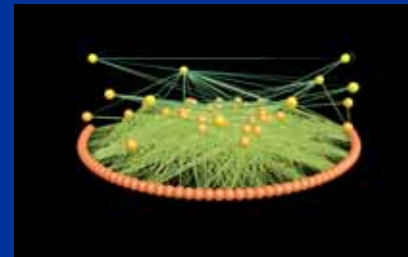
$C = 0.06$ ,  $S = 155$ ,  $L/S = 9.7$   
Waide & Reagan 1996

Canton Creek



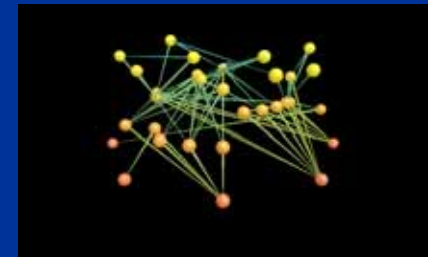
$C = 0.07$ ,  $S = 102$ ,  $L/S = 6.8$   
Townsend et al. 1998

Stony Stream



$C = 0.07$ ,  $S = 109$ ,  $L/S = 7.6$   
Townsend et al. 1998

Chesapeake Bay



$C = 0.07$ ,  $S = 31$ ,  $L/S = 2.2$   
Baird & Ulanowicz 1989



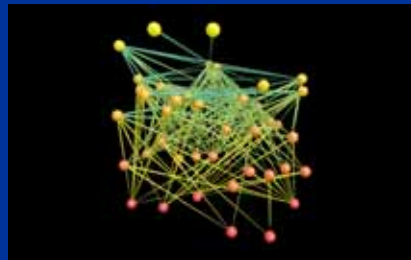
# Middle and High Connectance Webs, $C < 0.10$

St. Marks Seagrass



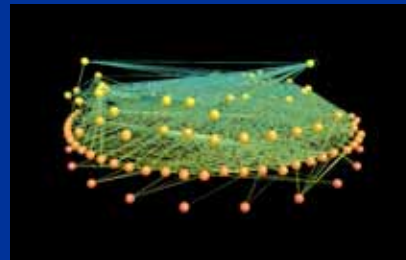
$C = 0.10$ ,  $S = 48$ ,  $L/S = 4.6$   
Christian & Luczkovich 1999

St. Martin Island



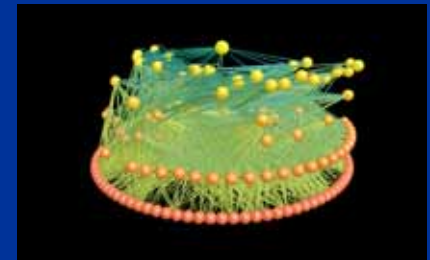
$C = 0.12$ ,  $S = 42$ ,  $L/S = 4.9$   
Goldwasser & Roughgarden 1993

Little Rock Lake



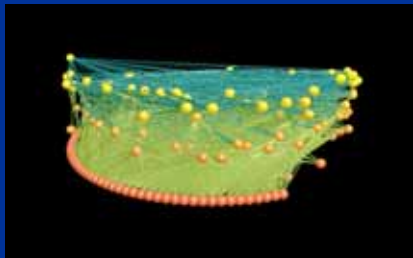
$C = 0.12$ ,  $S = 92$ ,  $L/S = 10.8$   
Martinez 1991

Lake Tahoe



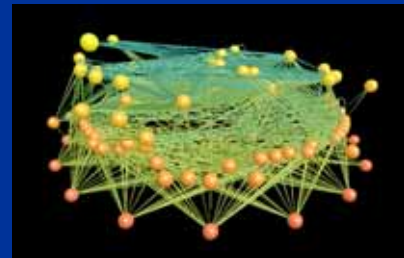
$C = 0.13$ ,  $S = 172$ ,  $L/S = 22.6$   
Vaccaro and Martinez unpubl.

Mirror Lake



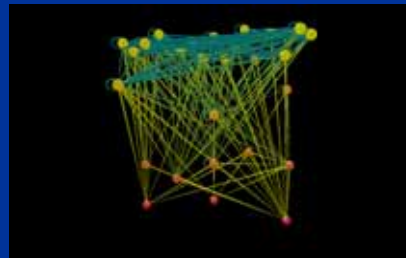
$C = 0.15$ ,  $S = 172$ ,  $L/S = 25.1$   
Puleston and Martinez unpubl.

East River



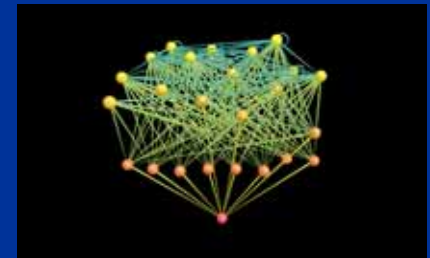
$C = 0.15$ ,  $S = 104$ ,  $L/S = 15$   
Harvey and Martinez unpubl.

Coachella Valley



$C = 0.31$ ,  $S = 29$ ,  $L/S = 9.0$   
Polis 1991

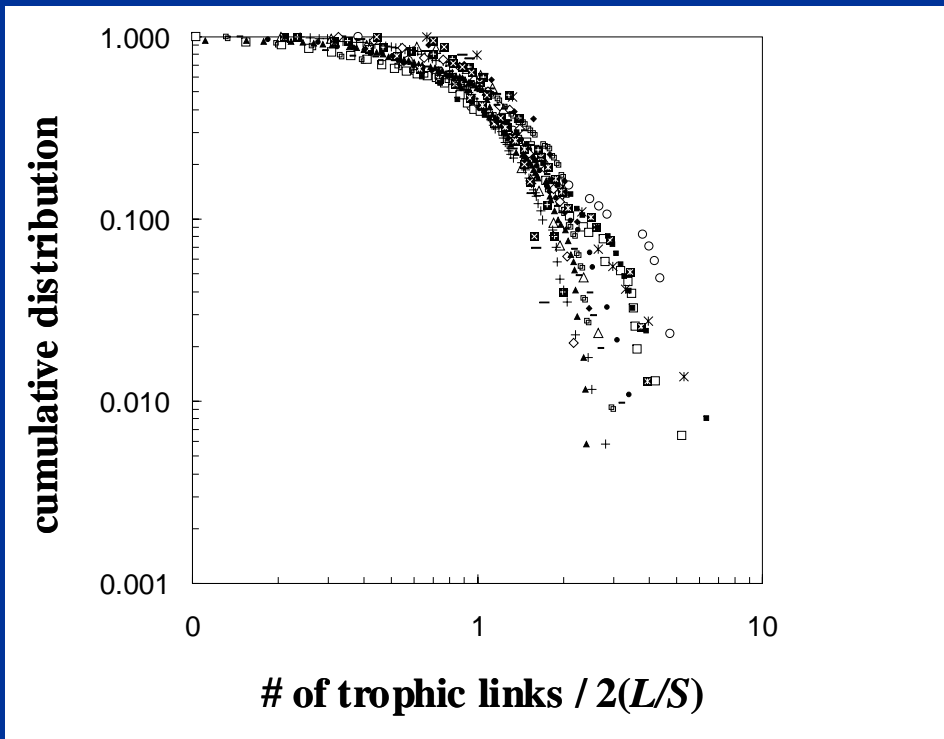
Skipwith Pond



$C = 0.32$ ,  $S = 25$ ,  $L/S = 7.9$   
Warren 1989



## Are food webs scale-free? Not really...



- Most food webs display single-scale (exponential or uniform) distributions. -i.e., no structurally 'over-dominant' taxa in food webs.
- The relatively high  $C$  and low  $S$  of food webs limits potential heterogeneity of feeding link distribution.

Dunne, Williams and Martinez

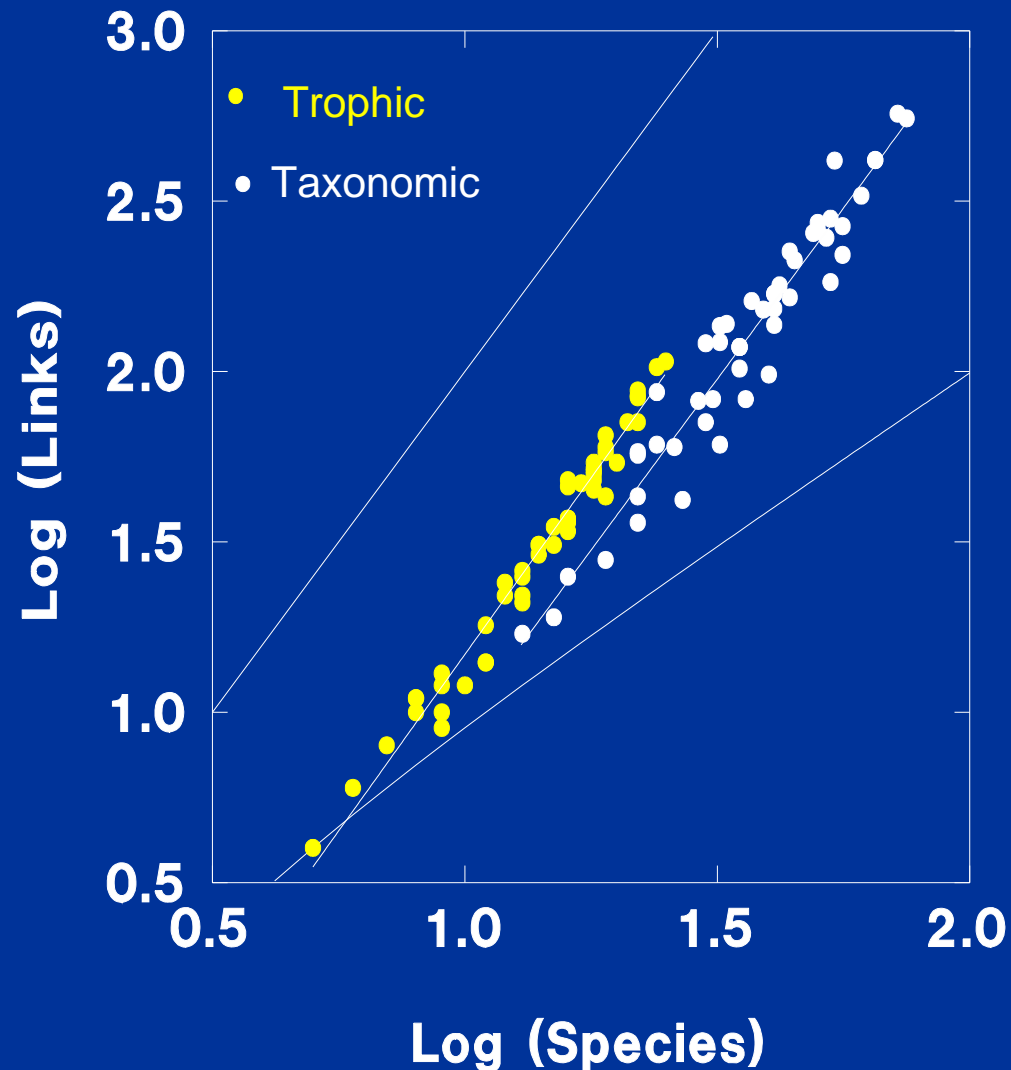
2002 *PNAS* 99:12917



# Constant Connectance ( $L/S^2$ ): $S$ is orthogonal to $L/S^2$

- Taxonomic webs
  - Slope = 2.01
  - $R^2 = 93\%$
- Trophic webs
  - Slope = 2.07
  - $R^2 = 97\%$

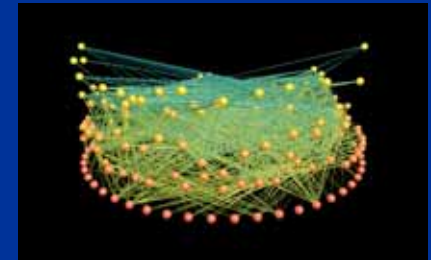
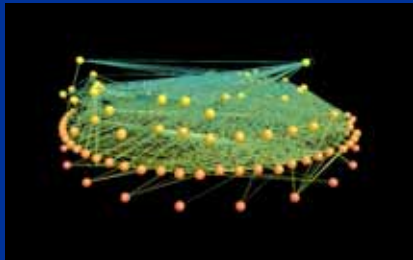
2 Versions of Havens'  
50 Pelagic Food Webs  
Martinez *Science* 1993





## Challenge

Which structural properties enable network persistence

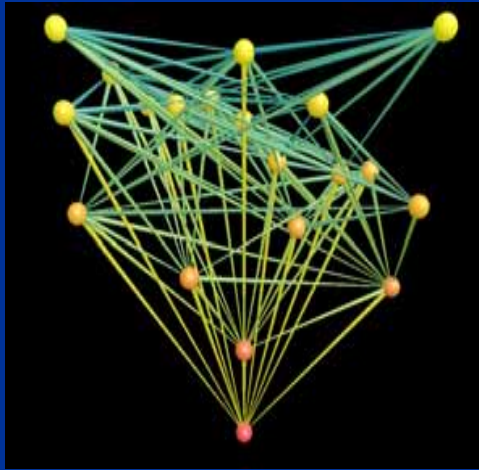


Analyses by an ecoinformatics approach that synthesizes

- (1) structural models of food webs and
- (2) allometrically scaling population dynamics



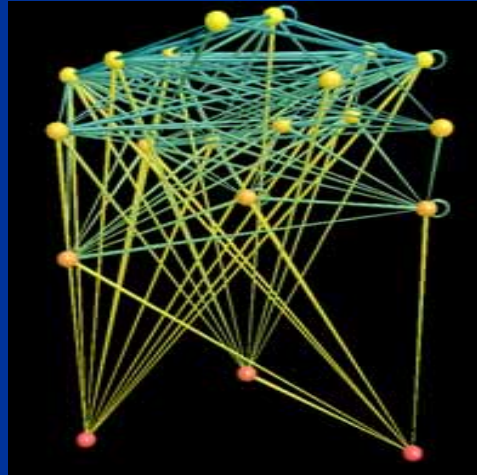
# Structural models of complex food webs



Cascade model

Cohen et al. 1990

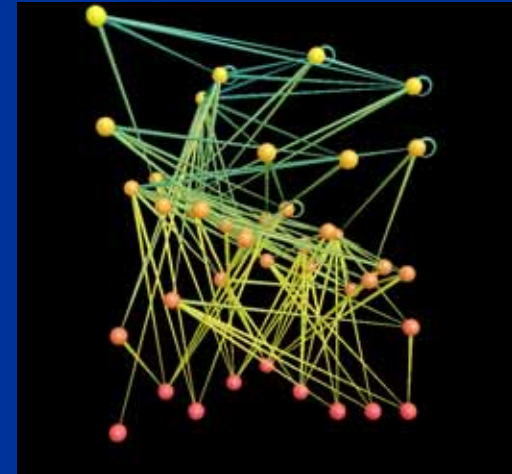
Strong trophic  
hierarchy



Niche model

Williams & Martinez 2000  
*Nature*

Looping allowed,  
contiguity required



Nested-hierarchy  
model

Cattin et al. 2004 *Nature*

Phylogenetic  
grouping and  
adaptation



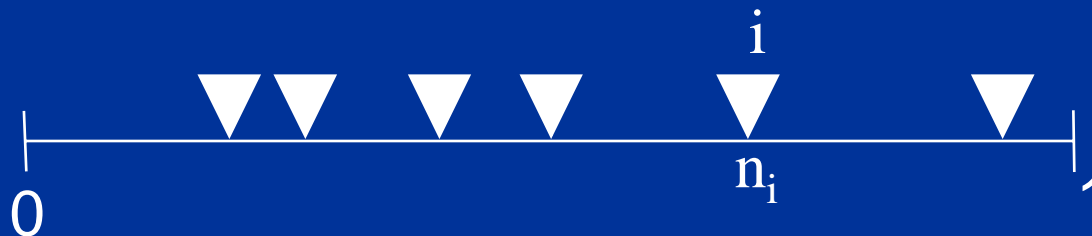
# Niche Model: Simple Rules

- Inputs: Diversity and Complexity (S & C)
  - Ecological contingency
- 3 Simple Rules



# Niche Model Rule 1

- Fixed one-dimensional community niche space
- Each species given a fixed location or “niche value”
- **Rule 1: Assign each of  $S$  species a uniformly random number  $[0, 1]$  so that the “niche value” of  $S_i$  is  $n_i$**





# Niche Model

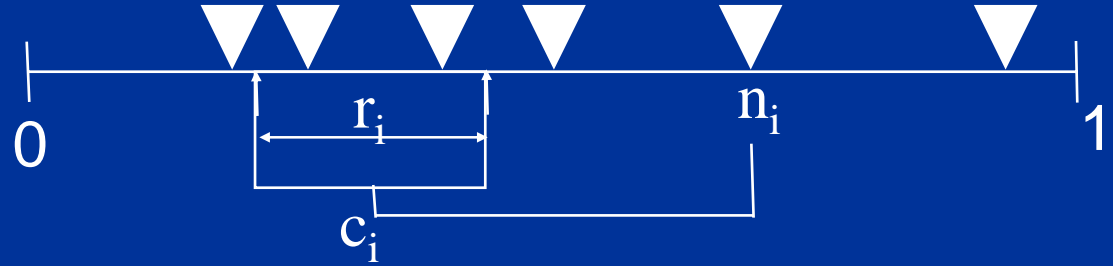
## Rule 2



- Rule 1: Each species gets uniform random  $n_i$
- **Rule 2: Each species gets assigned a random “feeding range” ( $r_i$ )  $0 \leq r_i \leq 1$** 
  - chosen from a beta function (mean of  $2C$ ) multiplied by the species niche value ( $n_i$ ).
- Stochastically distributes generality among species while ensuring web has comparable  $C$

# Niche Model

## Final Step 3

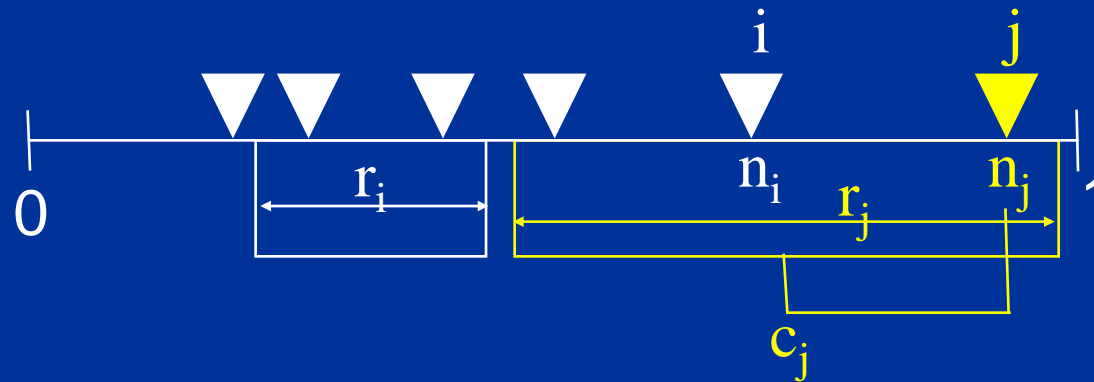


- Step 1: Each species gets uniform random  $n_i$
- Step 2: Each species gets beta random  $r_i$
- **Step 3: Each niche range is placed by uniformly choosing a random range center ( $c_i$ ) so that  $r_i/2 < c_i < n_i$**
- Establishes relaxed trophic hierarchy while allowing cannibalism and looping





## Niche Model: Mechanics



- Randomly assign “ $j$ ” species a niche value ( $n_j$ )
- Randomly assign species a niche range ( $r_j$ )
- Randomly assign the center of the range ( $c_j$ )
  
- Repeat 1000 times with observed  $S$  and  $C$



# Nested Hierarchy Model

- Inputs: Diversity and Complexity (S & C)
  - Ecological contingency
- Phylogenetic Adaptation
  - Species get beta-distributed diets
  - Starting with lowest ranked species, Species join feeding guilds that consume lower ranked species
  - If needed, more prey are randomly added



# Bioenergetic Nonlinear Population Dynamics

Biomass change  $\sim$  growth – metabolism + consumption – being consumed

$$B_i'(t) = r_i G_i(\vec{B}) - x_i B_i(t) + \sum_{j=1}^n (x_i y_{ij} F_{ij}(\vec{B}) B_i(t) - x_j y_{ji} F_{ji}(\vec{B}) B_j(t) / e_{ji})$$

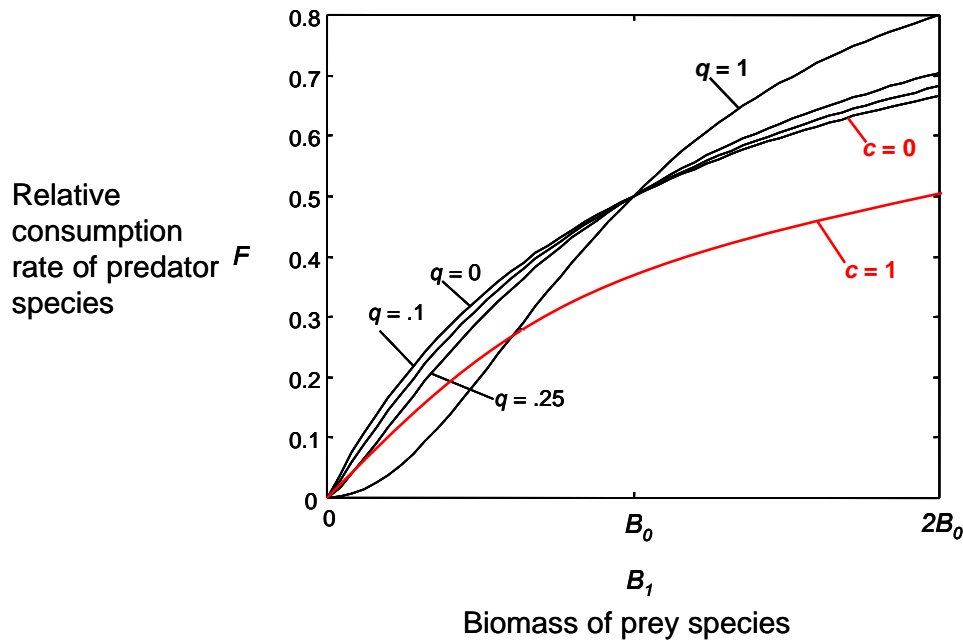
Growth rate

Metabolic rate

Maximum consumption rate

Functional response

## Gradation from Type II to Type III Functional Response



Addition of Predator Interference to Type II Functional Response:

$$F_{ij}(B) = \frac{B_j(t)^{1+q_{ij}}}{\sum_{k=1}^n \alpha_{ik} B_k(t)^{1+q_{ij}} + B_{0ji}^{1+q_{ij}}}$$

$\alpha$ : relative prey preference of predator species

$B$ : biomass

$B_0$ : half saturation density of prey species when consumed by predator species

$q$ : controls form of functional response

$q = 0$  (Type II)

$q = 1$  (Type III)

$$F_{ij}(B) = \frac{B_j(t)}{\sum_{k=1}^n \alpha_{ik} B_k(t) + (1 + c_{ij} B_i(t)) B_{0ji}}$$



## Bioenergetic Nonlinear Population Dynamics

Biomass change  $\sim$  growth – metabolism + consumption – being consumed

$$B_i'(t) = r_i G_i(\bar{B}) - x_i B_i(t) + \sum_{j=1}^n (x_i y_{ij} F_{ij}(\bar{B}) B_i(t) - x_j y_{ji} F_{ji}(\bar{B}) B_j(t) / e_{ji})$$

Growth  
rate

Metabolic  
rate

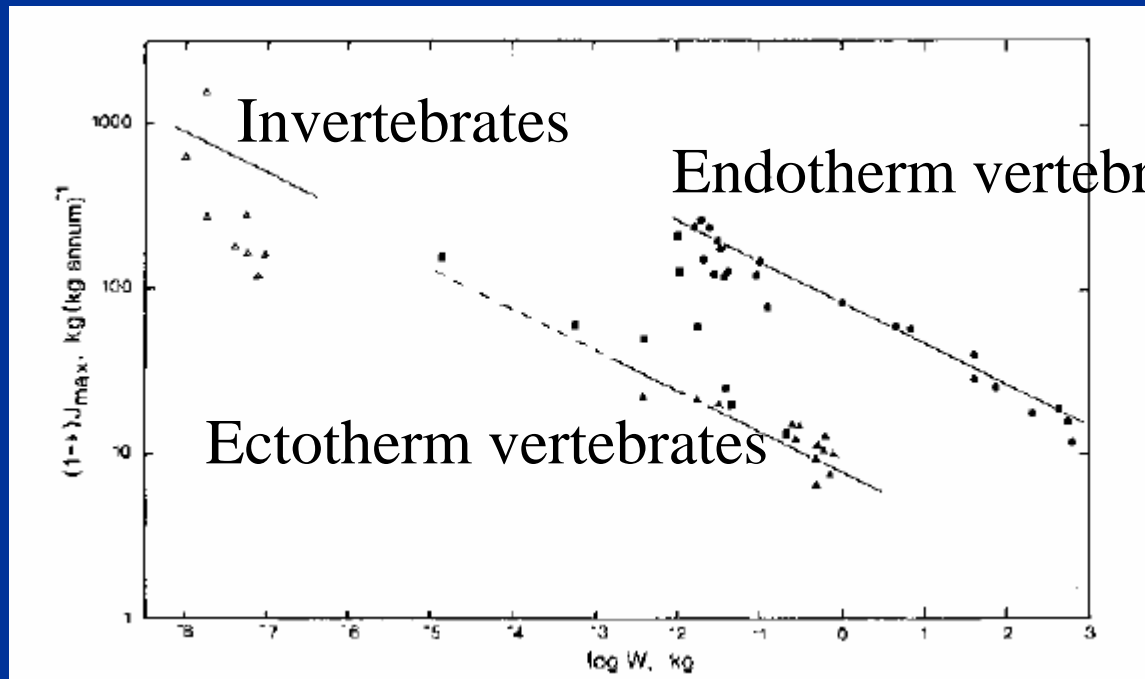
Maximum  
consumption rate

Functional  
response

Biological rates scale with a negative quarter power-law with species' body masses (West et al. 1997 *Science*, Enquist et al. 1999 *Nature*, West et al 1999 *Nature*)



## Power law allometric scaling relationships



From: Yodzis & Innes  
1992 Am. Nat.

Different metabolic types of species:

- same negative quarter exponent
- different allometric constants



Generate binary network with structural network model



Scale biological rates with negative quarter power-law



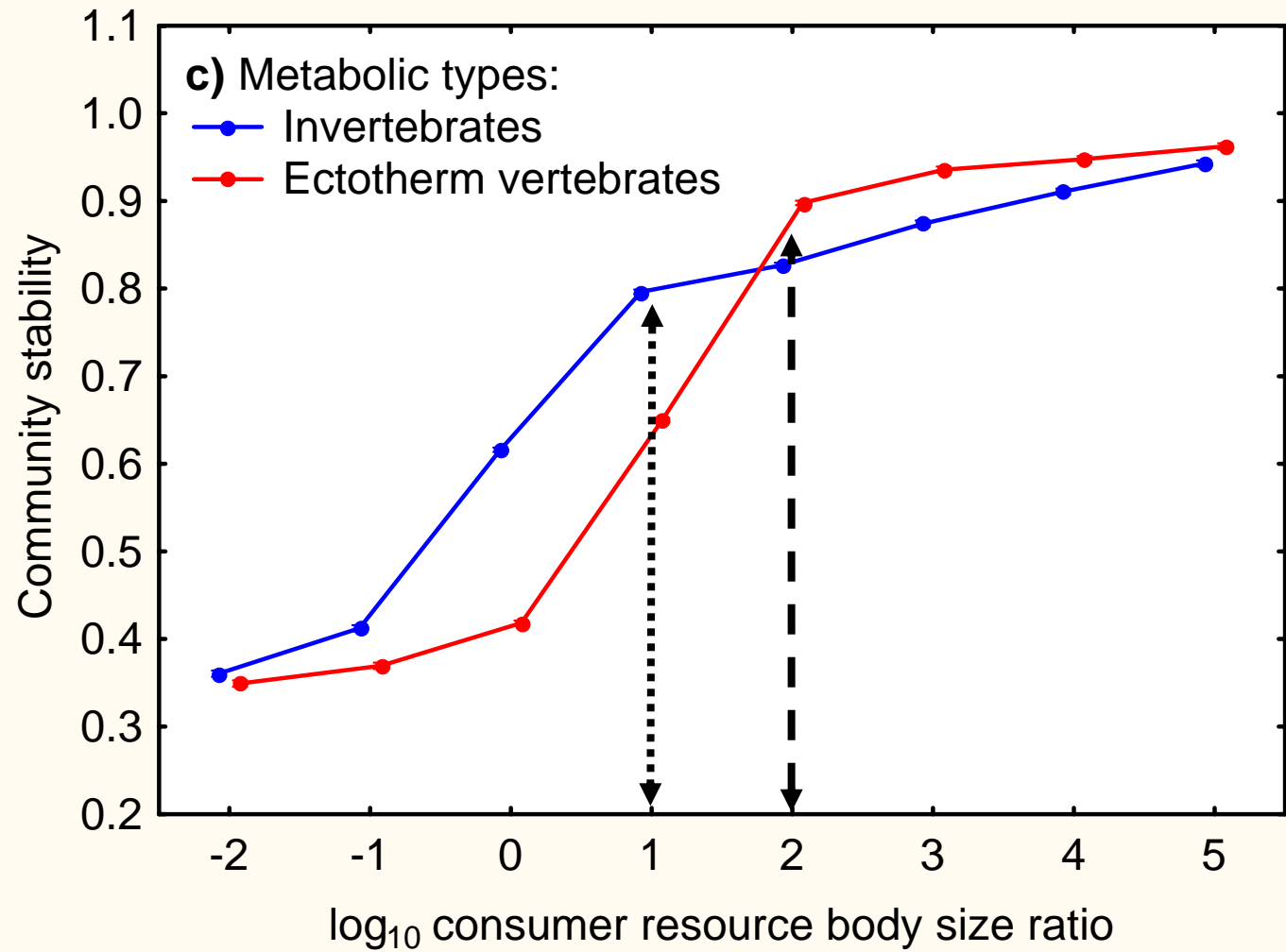
Parameterize network model of population dynamics



Simulate nonlinear population dynamics



Measure stability as probability of species persistence

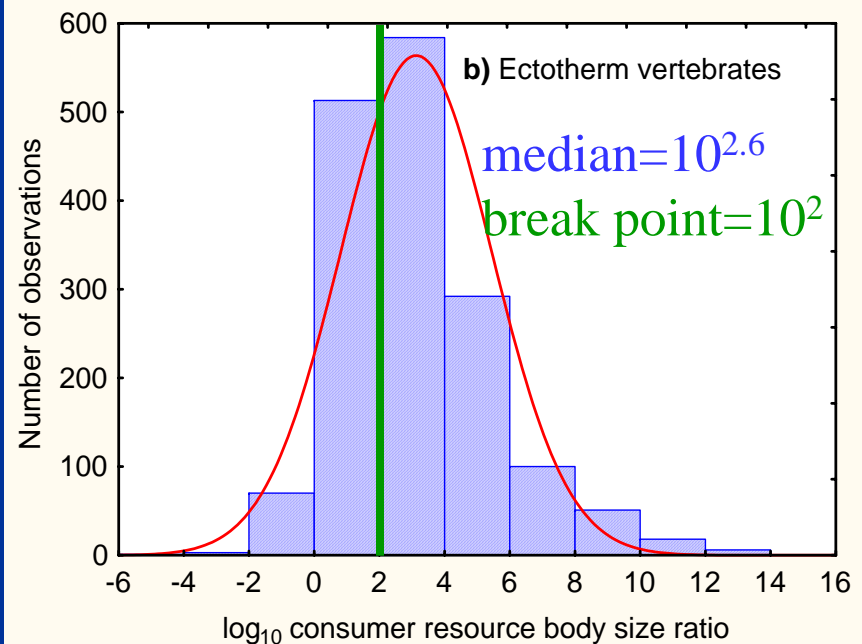
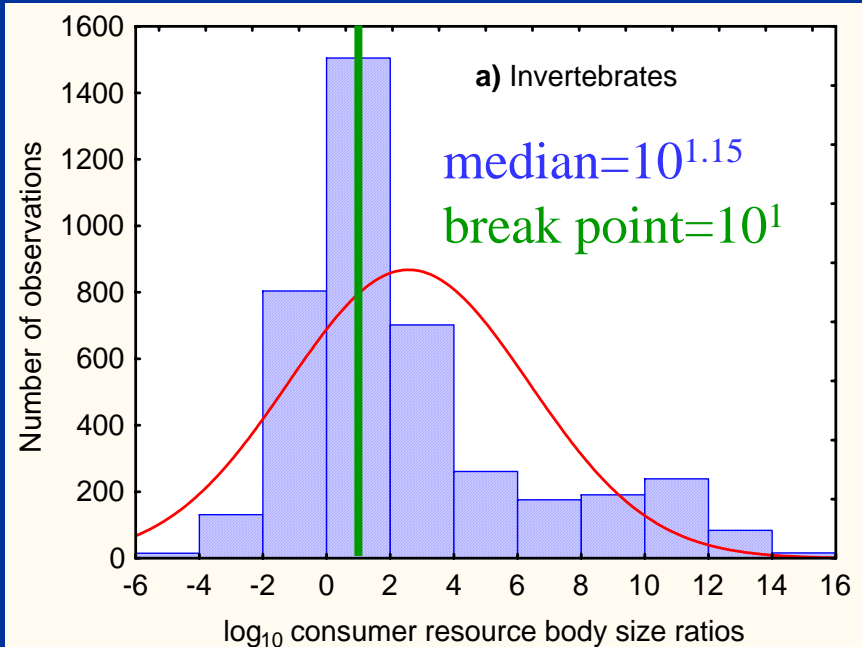


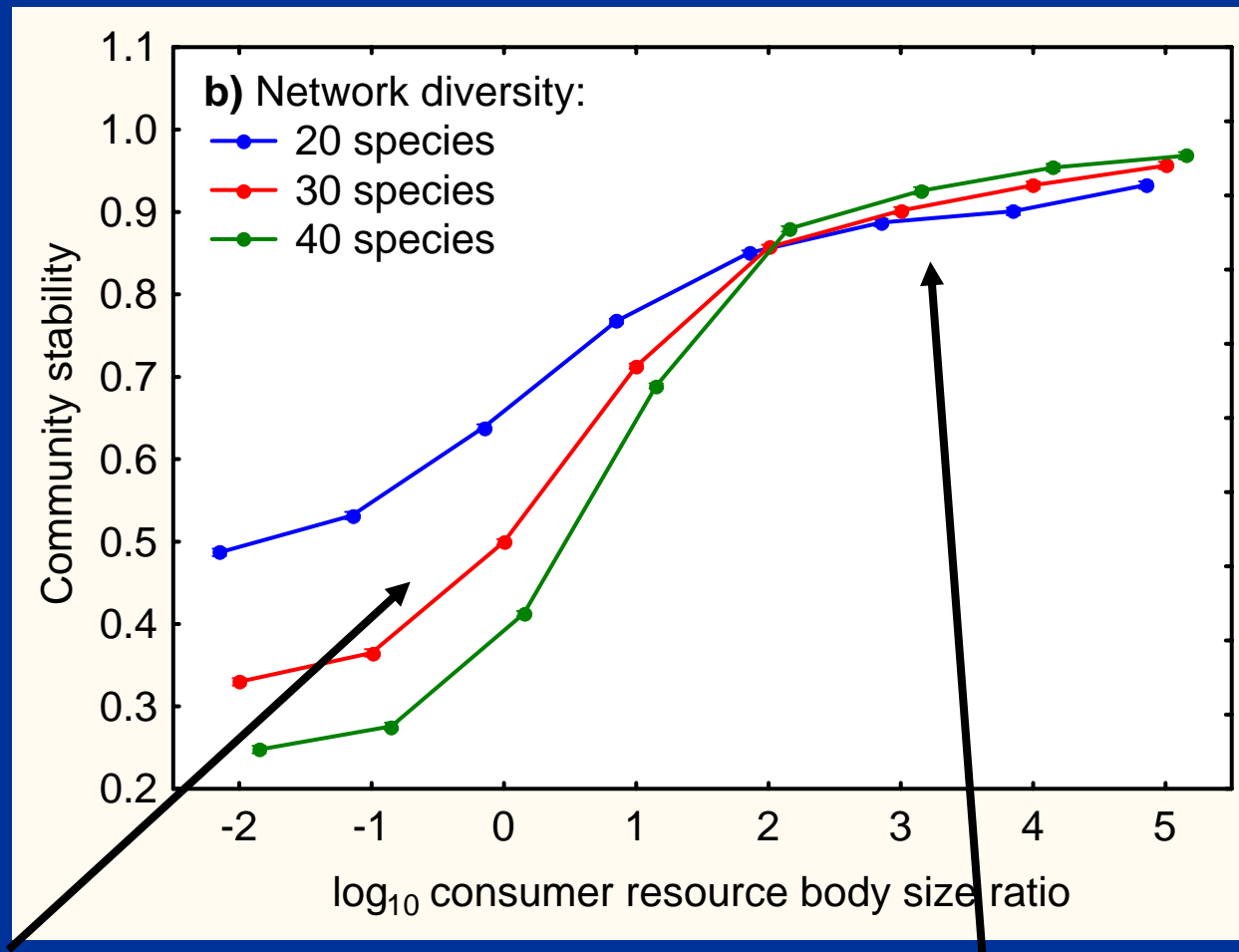


Global data base on natural  
body size ratios

Data for 3887 invertebrate  
predators and 1501 ectotherm  
vertebrate predators

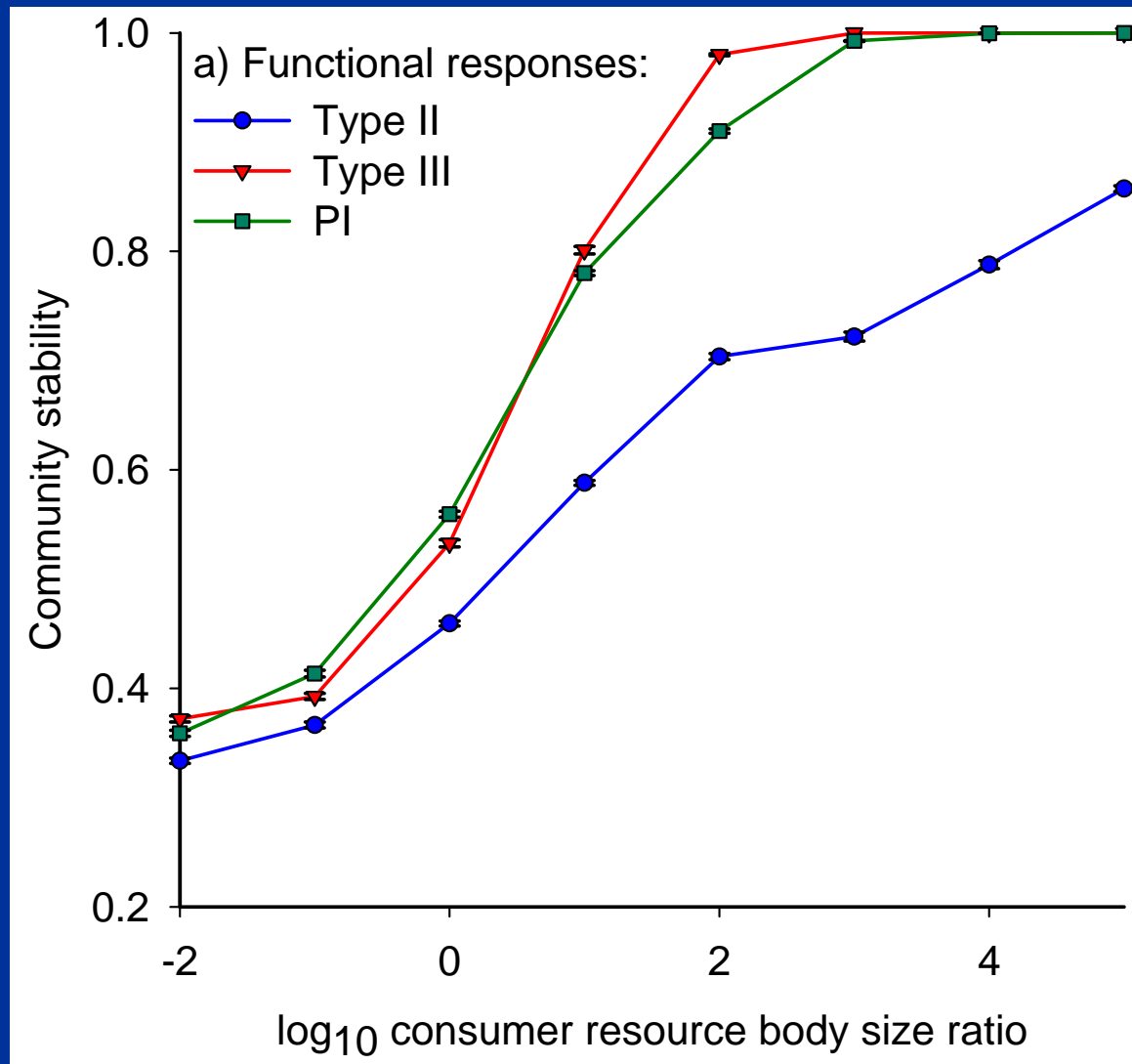
Geometric mean body size  
ratios are above break points



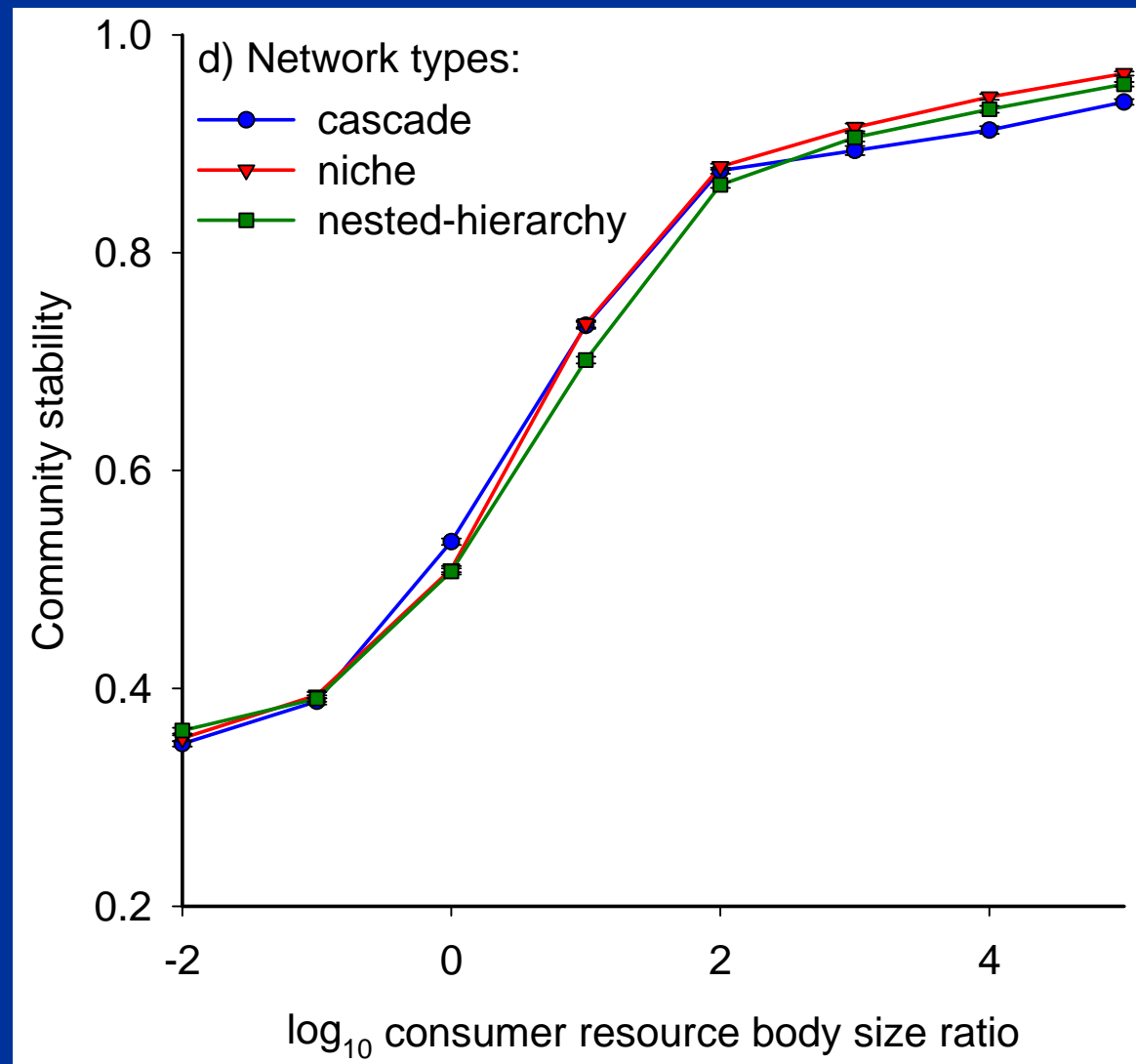


Negative diversity stability relationships under uniform body size distributions

Positive diversity stability relationships under natural body size distributions



**Results qualitatively robust to variation in Functional Responses**



**Results generally robust to limited variation in Network Structure**



## Conclusions - Part I

- Instability under abstract (random) dynamics on abstract (random) networks
- Stability under realistic (allometrically scaled) dynamics on realistic (non-random) networks
- Natural ecosystems are stabilized by their body size structure
- Including empirical realism allows simulation of complex ecological network dynamics – So where do we get the data? How can more scientists contribute to and conduct such simulations?
  - INFORMATICS!



## Conclusions Part II & Future Directions

- Ecoinformatics are Key to Computational and Basic Ecology
- Improve empirical estimates of maximum consumption rates, especially for invertebrates
- Empirically explore functional responses, especially variability within food webs
- *In Silico* explorations of network structure
- Improve and implement “data forever” ecoinformatics

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- **Scaling of Network Complexity with Diversity in Food Webs**
- **Webs on the Web: Internet Database, Analysis and Visualization of Ecological Networks**
- **Science on the Semantic Web: Prototypes in Bioinformatics**

Williams, R. J. and N. D. Martinez . 2000.  
Simple rules yield complex food webs. *Nature* 404:180-183.

Williams, R. J., E. L. Berlow, J. A. Dunne, A-L Barabási. and N. D. Martinez. 2002.  
Two degrees of Separation in Complex Food Webs. *PNAS* 99:12917-12922

Brose, U., R.J. Williams, and N.D. Martinez. 2003.  
The Niche model recovers the negative complexity-stability relationship effect in adaptive food webs.  
*Science* 301:918b-919b

Brose, U., A. Ostling, K. Harrison and N. D. Martinez. 2004.  
Unified spatial scaling of species and their trophic interactions. *Nature* 428:167-171

Williams, R.J., and N.D. Martinez. 2004.  
Limits to trophic levels and omnivory in complex food webs: theory and data.  
*American Naturalist* 163: 458-468

Williams, R. J. and N. D. Martinez . 2004. Stabilization of  
Chaotic and Non-permanent Food-web Dynamics. *Eur. Phys. J. B* 38:297-303

Brose, U., L. Cushing, E.L. Berlow, T. Jonsson, C. Banasek-Richter, L-F. Bersier, J.L. Blanchard, T. Brey, S.R. Carpenter, M-F. Cattin-Blandenier, J.E. Cohen, H.A. Dawah, A. Dell, F. Edwards, S. Harper-Smith, U. Jacob, R.A. Knapp, M.E. Ledger, J. Memmott, K. Mintenbeck, J.K. Pinnegar, B.C. Rall, T. Rayner, L. Ruess, W. Ulrich, P.H. Warren, R.J. Williams, G. Woodward, P. Yodzis, and N.D. Martinez. 2005. Body sizes of consumers and their resources. *Ecology* 86:2545.

